

Your signature _____

Show your steps. and work on another piece of paper. Each question is scored: 2 points for the correct answer; 3 points for the correct work. Partial credit may be awarded.

Solve.

$$\begin{aligned} 1) \quad & x^2 + 2y^2 = 11 \\ & x - y = 3 \end{aligned}$$

Solve the exponential equation. Round to three decimal places when necessary.

$$2) e^x + e^{-x} = 4$$

Find the average rate of change of the function over the given interval.

$$3) h(t) = \sin(3t), \left[0, \frac{\pi}{6}\right]$$

Solve, finding all solutions. Remember to use the "k" expression.

$$4) 2 \tan^2 x - 3 \sec x = 0$$

Solve the logarithmic equation.

$$5) \ln(5x - 1) = \ln 6 - \ln(x - 6)$$

Solve.

$$6) 4x^3 - 15x^2 \leq 25x$$

Find the value of the constant k that makes the function continuous.

$$7) h(x) = \begin{cases} \frac{7x^2 + 25x - 12}{x + 4} & \text{if } x \neq -4 \\ 4x + k & \text{if } x = -4 \end{cases}$$

Find the slope of $f(x)$ at the given value of x . Make sure to write a limit expression. Use one of the definitions of the derivative

$$8) f(x) = \frac{-1}{x + 6}; \quad x = -4$$

Find the values of x where the piecewise defined function is NOT continuous or NOT differentiable. Identify the types of discontinuities.

$$9) \quad f(x) = \begin{cases} e^{-x} - 5, & \text{for } x < -2, \\ x - 1, & \text{for } -2 \leq x < 1 \\ x^3, & \text{for } x \geq 1 \end{cases}$$

Find the limit, if it exists.

$$10) \lim_{x \rightarrow 0} \frac{\sqrt{1+x} - 1}{x}$$