

Your signature _____

Show your steps. and work on another piece of paper. Each question is scored: 2 points for the correct answer; 3 points for the correct work. Partial credit may be awarded.

Solve.

$$\begin{aligned} 1) \quad & x^2 + 2y^2 = 11 \\ & x - y = -3 \end{aligned}$$

Solve the equation for the interval $[0, 2\pi)$.

$$2) \sin^2 x - \cos^2 x = 0$$

Prove the identity.

$$3) \tan^2 x + \cos 2x = 1 - \cos 2x \tan^2 x$$

Solve the exponential equation. Round to three decimal places when necessary.

$$4) e^x + e^{-x} = 5$$

Solve the logarithmic equation.

$$5) \ln(5x - 4) = \ln 4 - \ln(x - 1)$$

Solve.

$$6) 3x^3 - 11x^2 \leq 20x$$

Find the average rate of change for the function over the given interval.

$$7) y = x^3 + x^2 - 8x - 7 \quad \text{between } x = 0 \text{ and } x = 2$$

Use the formula for instantaneous rate of change, approximating the limit by using smaller and smaller values of h , to find the instantaneous rate of change for the function at the given value. This is a tabular solution.

$$8) \text{ Approximate the instantaneous rate of change of } f(x) = x^{1/x} \text{ at } x = 3. \text{ Explain what you did.}$$

Find the limit, if it exists.

$$9) \lim_{h \rightarrow 0} \frac{2}{\sqrt{3h+4} + 2}$$

$$10) \lim_{x \rightarrow 1} \frac{x^4 - 1}{x - 1}$$