

Practice Exam 1 Review

This is NOT intended to be comprehensive!

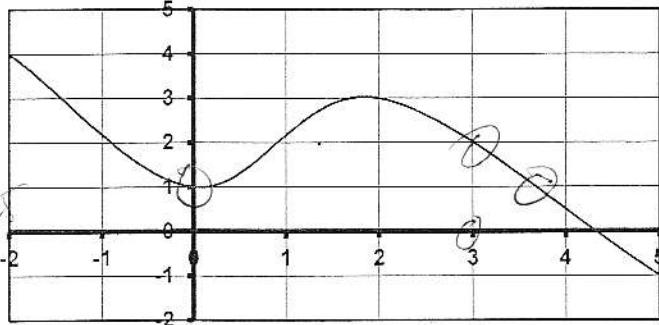
- 1) Below is shown the graph of  $f(x)$

- a) Evaluate  $f(3)$   
b) Solve  $f(x) = 1$

$$f(3) = 2$$

⑤ what is when

$$y=1 \quad x=0 \text{ and } x=3$$



- 2) Suppose the function  $A(t)$  gives the height of an airplane (in feet)  $t$  minutes after takeoff.

- a) Interpret  $A(5)$   
b) Suppose you solve  $A(t) = 300$ . What is the meaning of your solution?

- 3) Given the function  $f(x)$  defined by the table below,

$x$	1	2	3	4	5	6	7	8
$f(x)$	2	4	5	6	5	3	-2	-1
$g(x)$	8	1	3	2	7	6	4	5

- a) Evaluate  $f(6)$   
b) Solve  $f(x) = 4$   
c) Evaluate  $g^{-1}(7)$   
d) Evaluate  $f(g(7))$   
e) Evaluate  $g(f(1))$

- 4) Suppose the following table shows the cost of a latte, in dollars, as a function of the size of the latte, in ounces.

$s$	8	12	16	20
$C(s)$	2.0	2.5	3.0	3.5

- a) Evaluate  $C(12)$  and give its meaning in practical terms  
b) Solve  $C(s) = 3.0$  and give its meaning in practical terms

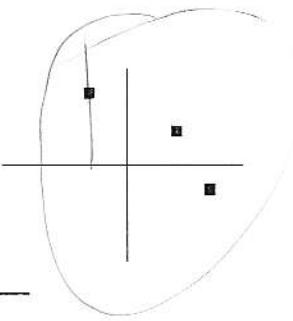
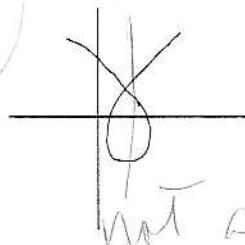
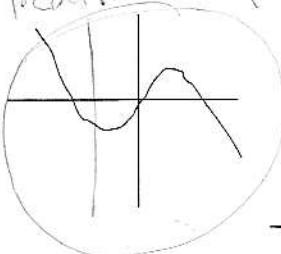
- 5) Circle all of the following that represent functions

in	1	4	6	4
out	2	5	6	1

in	2	3	5	4
out	3	5	6	5

in	2	4	6	7
out	5	7	6	4

X represents F(4) = 2



not a function

(2) (a) The ht of the airplane 5 min.  
after take off

(b) The times when the plane is 300ft up  
↓  
minutes after take off

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(3)  $f(6) = 3$

$F(x) = 4 \quad x = 2$

$g^{-1}(7) = g(x) = 7 \quad x = 5$

$f(g(7)) \quad g(7) = 4 \quad f(4) = 6$

$g(f(1)) \quad f(1) = 2 \quad g(2) = 1$

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(4) (a) The cost of a 12 oz latte

(b) \$16 oz This how much a  
16 oz latte costs (\$3.00)

Sounds cheap to me!

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(5) See Paper

6) Given  $f(x) = \frac{-2}{x+4}$

- a) Evaluate  $f(3)$
- b) Evaluate  $f^{-1}(6)$
- c) State the domain of  $f(x)$
- d) Evaluate  $f(c - 1)$
- e) Given  $g(x) = x^2 - 1$ , find  $f(g(x))$

Wet Pg

7) Find the domain of the following functions

a)  $h(t) = \sqrt{3 - 2t} + 1$

b)  $g(x) = \frac{x-3}{x-5}$



8) Determine the domain and range of the following function and sketch its graph

$$f(x) = \begin{cases} -3 & x < -1 \\ 3x & -1 \leq x \leq 1 \\ 3 & x > 1 \end{cases}$$



9) Given a function  $f(x)$ , represent the following in function notation

a)  $f(x)$  shifted 3 units to the left

$$F(x+3)$$

b)  $f(x)$  flipped over the  $y$  axis

$$F(-x)$$

c)  $f(x)$  stretched horizontally by a factor of 2

$$F\left(\frac{1}{2}x\right)$$

$$\frac{1}{2}F(x)$$

d)  $f(x)$  compresses vertically by a factor of 1/2

$$\frac{1}{2}F(x)$$

e)  $f(x)$  compressed horizontally by a factor of 1/2

$$F(2x)$$

f)  $f(x)$  stretched vertically by a factor of 2

$$\rightarrow 2F(x)$$

g)  $f(x)$  shifted down 2 units

$$F(x) - 2$$

h)  $f(x)$  shifted right 5 units

$$F(x-5)$$

i)  $f(x)$  flipped over the  $x$ -axis

$$-F(x)$$

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$$\textcircled{c} \textcircled{a} f(3) = \frac{-2}{3+4} \rightarrow \textcircled{\frac{-2}{7}}$$

$$\textcircled{b} \quad f(x) = 6 \quad \frac{6}{1} = \frac{-2}{x+4} \quad \text{a proportion}$$

$$\textcircled{c} \quad x \neq -4$$

or

$$6(x+4) = -2$$

$$(-\infty, -4) \cup (-4, \infty)$$

$$6x = -26$$

$$x = -\frac{26}{6}$$

$$\textcircled{-\frac{13}{3}}$$

$$\textcircled{d} \quad f(c-1) = \frac{-2}{c-1+4} \rightarrow \textcircled{\frac{-2}{c+3}}$$

$$\textcircled{e} \quad f(x^2-1) = \frac{-2}{x^2-1+4} \rightarrow \textcircled{\frac{-2}{x^2+3}}$$

$$\textcircled{f} \textcircled{a} \quad 3-2t \geq 0$$

$$\therefore t \leq \frac{3}{2} \quad \text{or} \quad (-\infty, \frac{3}{2}]$$

$$\textcircled{b} \quad x-5=0 \quad \text{or} \quad (-\infty, 5) \cup (5, \infty)$$

$$x \neq 5$$

⑧

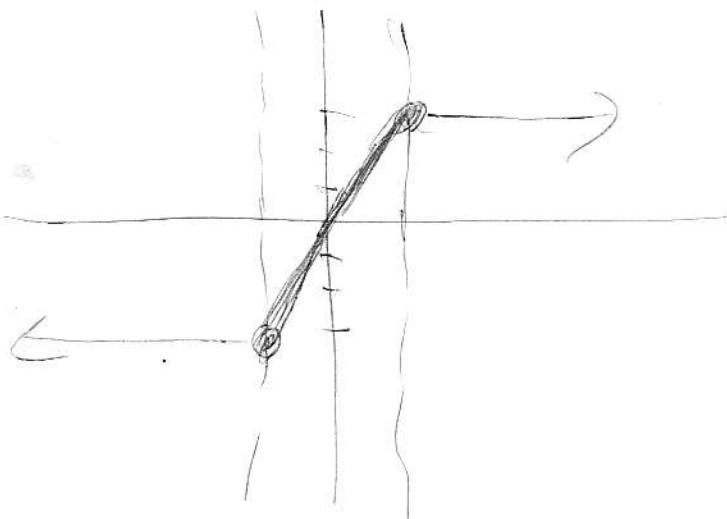
Range  $[3, \infty]$

Domain all reals

$$3x+0$$

$$\text{slope} = \frac{3}{1}$$

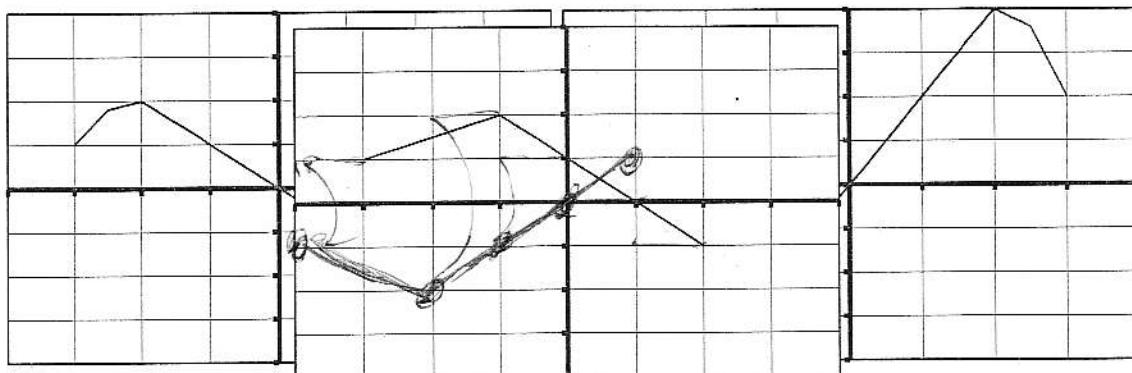
$$y\text{-int} = (0, 0)$$



Def

10) Describe in words the following transformation:  $-3f(x - 2) + 1$

11) Graphed below is the function  $g(x)$  and a transformation of  $g(x)$ . Write an equation for the transformation.



12) Shown below is a graph of  $f(x)$ . Sketch a graph of  $-f(x + 1)$

Left }  
reflected about x-axis

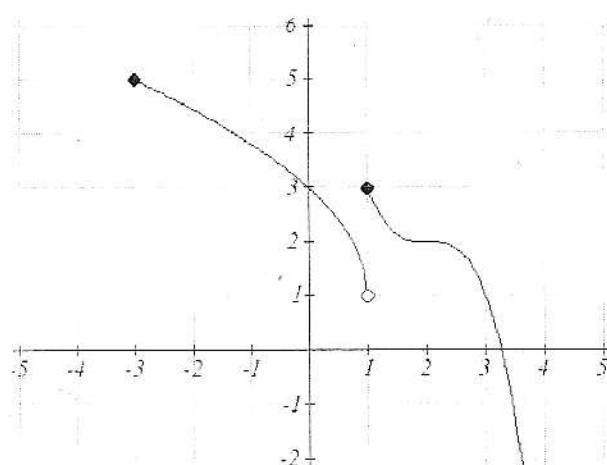
13) Suppose the function  $f(a)$  gives the amount of tax owed by a person with an income of  $a$ . Write in function notation:

- I paid \$100 less in taxes than I owed
- Because of a deduction, I had to pay taxes on \$100 less than my income.

14) Write an equation for the piecewise function graphed below.

Hint: it is comprised of two transformed toolkits.

$$\begin{cases} 2\sqrt{x-1} + 1 & \text{on } [-3, 1] \\ (x-2)^3 + 2 & \text{on } [1, \infty) \end{cases}$$



(10) Shifted Right 2  
Stretched vertically by a factor 3  
reflected around the x-axis  
Shifted up 1

(11) All messed up

(12) Not middle graph  
See paper

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(13) a)  $f(a) - 100$  — Tax credit.  
b)  $F(a - 100)$  — Tax deduction

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(14) on Paper