

# Data Key Practice Examples

① Proportions       $n=50$        $\hat{P} = \frac{35}{50} = 0.7$

Critical value of  $Z^* = 1.96$

$$0.7 \pm 1.96 \sqrt{\frac{0.7(0.3)}{50}}$$

$$0.7 \pm 1.96 (0.065)$$

$$0.7 \pm 0.127 \rightarrow 0.573 \text{ to } 0.827$$

using STAT > TEST > 1-Prop Z INT

$$(0.57298, 0.82702)$$

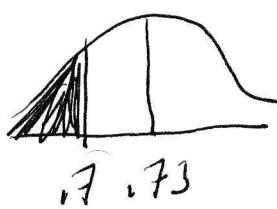
We are 95% confident the true percentage of her students registered to vote is between 57.3% to 82.7%.

② Proportions       $50(.73) > 10$        $50(.27) > 10$  Random

so ok to run a 1 prop z test

$$H_0: P = 0.73 \text{ The claim}$$

$$H_1: P < 0.7$$



Test statistic

$$Z = \frac{0.7 - 0.73}{\sqrt{0.73(0.27)/50}} = \frac{-0.03}{0.063} \rightarrow -0.48$$

$$P\text{-value} = .314$$

@ the 5% level of sig.  
we fail to reject H0

2 continued from the "flow chart"

There is not sufficient evidence to warrant the rejection of the claim that the true percentage of students @ this school who are registered to vote is different from the national percentage

$$(3) n = \left( \frac{1.96 (.73)(.27)}{.04} \right)^2 = 94$$

or something like that,

- (4) State that the percentage of students registered to vote in her class is lower than the Gallup Poll results, when really the students are just as politically active (the same percent registered to vote) as the national figure.

- 
- (5) Claim The percentage of Black Americans who can't afford health care is lower than the national percentage

Conditions Random ✓

$$801 (.28) > 10$$
$$801 (.72) > 10$$

$$H_0: P = .28$$

H<sub>a</sub>: P < .28 or maybe P ≠ .28 claim

5 confidence

$$Z = \frac{.38 - .28}{\sqrt{\frac{.28(.72)}{801}}} \rightarrow \frac{.1}{.016} \rightarrow 6.30$$

P-value essentially 0 whether a Two Tailed Test or a one tailed test. Rejects the sample data support the claim that the percentage of Black Americans who can't afford health care is different than the national percentage or something like that.

- ⑥ Failing to reject  $H_0$  when we should fail to say that the proportion of Black Americans that can afford healthcare is NOT different from all Americans, when actually this proportion is different.

$$\textcircled{7} \quad 0.38 \pm 1.96 \sqrt{\frac{.38(.72)}{801}} \\ 0.38 \pm 0.036 \rightarrow (0.344, 0.416)$$

We are 95% confident the true ~~proportion~~ <sup>Percentage</sup> of Black Americans who have not been able to afford health care during the past year is between 34.4%, to 41.6%.

$$\textcircled{8} \quad n = \left( \frac{1.96 (.25)}{.03} \right)^2 = \textcircled{267}$$

### \textcircled{9} Two proportion Z-test

Random, Both Samples

Claim: Higher rate of illiteracy among men in Qatar

$$H_0: P_m = P_w$$

$$X_m = 45 \quad X_w = 42$$

$$H_1: P_m > P_w \quad \text{The claim}$$

$$n_m = 234 \quad n_w = 251$$

using Software: Rosman-Chance 2 proportions

Graphing Calc STAT > TEST > 6:2-Prop ZTEST

$$\text{Test Statistic } Z = 0.72$$

$$p\text{-value} = 0.2369$$

@  $\alpha = 0.05$  Fail to reject  $H_0$

There is not sufficient evidence to support the claim that a higher rate of illiteracy exist among men in Qatar.

(13)

Matched Pairs 2 Dependent Samples.

Condition C.K Random Sample ✓

We don't know about Normality  $\{n < 30\}$

There are concerns about this test

Does C.L.T. hold?

$$H_0: \mu_d = 0$$

$H_1: \mu_d < 0$  & does anxiety decrease post course,

The claim:

1-sample T-test on differences

$$\bar{x}_d =$$

$$\text{TEST STATISTIC } T = -3.92$$

P-value - ,00067985 pretty small

@ any level of significance

Reject  $H_0$

The sample data support the claim  
that taking a statistics course does decrease  
anxiety about statistics.

(11) Continuous DK

2 - independent samples 2 Sample T-Test

Random Together more than 30 data points so probably  
OK to use Test

Claim Avg beats/min for dance songs is smaller  
than Avg beats/min for Top 200:

$H_0: \mu_D = \mu_{TOP}$  2 Sample T-Test

$H_1: \mu_D < \mu_{TOP}$  claim

TEST STATISTIC

$$T = -1.45$$

P-value = 0.079 @ 5% level of significance

Fail to reject  $H_0$

There is not sufficient sample evidence to support the claim that there ~~are~~ are fewer beats per minute, on average, in Dance Music vs Top 200 music.

(12) Categorical variable

$\chi^2$  GOF Test

$$n = 325$$

expected

$$A_S^e = 48.7$$

$$B_S^e = 97.8$$

$$C_S^e = 130$$

$$D_S^e = 32.5$$

$$F_S^e = 16.25$$

$H_0$ : Grade distribution is as expected

$H_1$ :  $H_0$  False

$$\chi^2 = 62.5 \quad P\text{-value} = 0$$

Test Statistic

Reject  $H_0$   
The sample data supports the claim. For this semester grade distribution does not match the historic record.

(13) Two-way-table Categorical Variables

$\chi^2$  test for independence

No counts  $< 5$

Expected Counts

	P. P	Made-in-U	25-hour
Rejected	57.7	51.5	61.8
Perfect	85.0	79.9	91.1
Acceptable	25.3	22.6	27.1

$H_0$ : No association between ~~Vendor~~ Vendor  
Quality of part

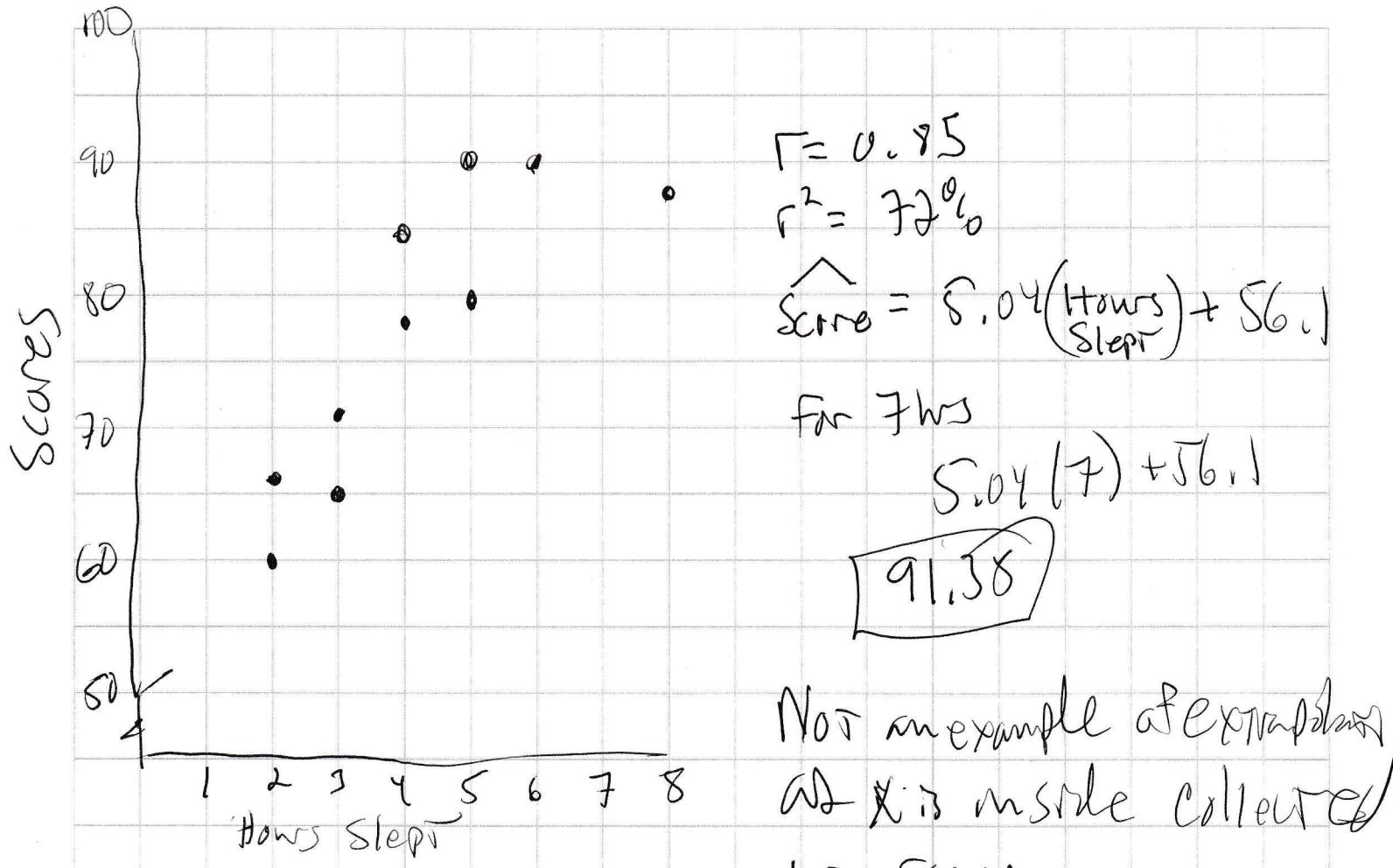
$H_1$ :  $H_0$  false (The claim)

TEST STAT

$$\chi^2 = 7.410 \quad p\text{-value} = 0.116$$

Fail to reject  $H_0$  at  $\alpha = 0.05$  level.

There is not sufficient sample evidence to support and claim that the defect rate is different at any one company.



Not an example of extrapolation  
 As  $x$  is outside collected data range.

We see a strong positive linear association.  $R$  is statistically significant at the 5% level. I'm ~~not~~ fairly confident this is a reasonable estimate.

